



CSCI 625: Program Synthesis and Computer-Aided Verification

Units: 4

Spring 2025—Mondays and Wednesdays—3:30—5:20pm
DMC 209

<https://r-mukund.github.io/teaching/sp2025-csci625/>

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Course Description

How does a programmer convince their colleagues that a piece of code does what was intended? How do they find bugs in the software they ship? And can the tools used for these activities also help in developing code that is correct, by construction?

This course will equip the student to answer these questions, and serve as an introduction to the principles and practices of software verification and program synthesis. We will study fundamental ideas such as symbolic execution, invariants, and abstract interpretation. We will also study how constraint solvers work, how they can be used to reason about code, and how they can be used as the building blocks of sophisticated program synthesis systems.

The course will cover both the theory underlying the design of these tools and their use in practice. Furthermore, by studying their application in areas such as networking and security, we will emphasize their relevance to the working computer scientist.

Learning Objectives

After this course, the successful student will be able to:

1. Prove properties of simple programs by devising appropriate invariants and ranking functions
2. Use constraint solvers to solve various problems
3. Explain the operation of modern constraint solvers, including unit propagation, back-tracking, clause learning, and theory combination
4. Explain the ideas behind abstract interpretation, including specific instantiations such as predicate abstraction and dataflow analyses
5. Implement simple static analyses for a tiny imperative programming language
6. Use and explain the operation of CEGIS-based program synthesizers

Prerequisites

1. The course will expect a certain amount of mathematical maturity from its students, at least at the level of CSCI 170, and preferably at the level of CSCI 270.
2. We will be reasoning about code: we expect that the student will already be proficient in writing it. CSCI 301, CSCI 350, and similar courses are appropriate baselines

Required Readings

We will assign readings from the following sources:

1. Michael Gordon. Background Reading on Hoare Logic. 2016.
Accessible from <https://www.cl.cam.ac.uk/archive/mjcg/HL/Notes/Notes.pdf>.
2. Daniel Kroening and Ofer Strichman. Decision Procedures: An Algorithmic Point of View. 2nd edition. Springer, 2016.
The book may be accessed freely from within USC at <http://link.springer.com/978-3-662-50497-0>. Supplementary material is available at <http://www.decision-procedures.org/>.

3. Anders Møller and Michael Schwartzbach. Static Program Analysis. Department of Computer Science, Aarhus University. 2018.
Accessible from <http://cs.au.dk/~amoeller/spa/>.
4. Susan Horwitz. Abstract Interpretation. 2013.
Accessible from <http://pages.cs.wisc.edu/~horwitz/CS704-NOTES/10.ABSTRACT-INTERPRETATION.html>.
5. Sumit Gulwani, Oleksandr Polozov, and Rishabh Singh. Program Synthesis. Foundations and Trends in Programming Languages, 2017.
Accessible from <https://ieeexplore.ieee.org/document/8187066>.

We will be supplementing this material with recent research papers.

Description and Assessment of Assignments

1. There will be four homework assignments. Each assignment will include a theoretical component to assess conceptual understanding and a practical component to provide familiarity with using verification and synthesis tools on real programs. Homeworks will be done independently.
2. Students will complete a small research project over the course of the semester. This project can be done either individually or in groups of two. They can either:
 - a. Find a new application of the verification and synthesis techniques presented in class, or
 - b. select a recent research paper and reimplement its algorithm.
 At the end of the semester, they will submit a report and present their findings to the class.

Students are strongly encouraged to consult the instructor while selecting an appropriate research project. In addition to the initial project proposal and final project report and presentation, it is recommended that they regularly update the instructor with their progress, both over email and during office hours.

Grading Breakdown

Assessment Tool (assignments)	Points	% of Grade
Assignment 1	100	20
Assignment 2	100	20
Assignment 3	100	20
Assignment 4	100	20
Research project	100	20
TOTAL	500	100

Course Schedule

Unit 1: Reasoning Engines

Reading: Chapters 2, 3 and 4 of (Kroening and Strichman, 2016).

Lab: Solving puzzles such as Sudoku, Kakuro, Numberlink and Slitherlink using Z3

Week 1	<ul style="list-style-type: none">• Course introduction, motivation, logistics• Propositional logic, satisfiability, and validity
Week 2	<ul style="list-style-type: none">• Basics of SAT solvers: DPLL, unit propagation, solving Horn-SAT in polynomial time• Solving 2-SAT in polynomial time
Week 3	<ul style="list-style-type: none">• Conflict-driven clause learning• Introduction to SMT: The DPLL(T) procedure
Week 4	<ul style="list-style-type: none">• Theory solvers: Difference logic, real arithmetic, uninterpreted functions• Combining theories using the Nelson-Oppen procedure

Unit 2: Program Synthesis

Reading: (Gulwani, Polozov and Singh, 2017)

Lab: Synthesizing program invariants using SyGuS

Week 5	<ul style="list-style-type: none">• Specifying user intent and syntactic bias• The Syntax-Guided Synthesis framework (SyGuS)
Week 6	<ul style="list-style-type: none">• Version spaces• Counter-example guided inductive synthesis (CEGIS)
Week 7	<ul style="list-style-type: none">• Instantiations of the CEGIS method: Enumerative, stochastic, and symbolic synthesis

Unit 3: Proof Techniques

Reading: Chapters 1, 2 and 5 of (Gordon, 2016).

Lab: Verifying simple programs using the Boogie IVL

Week 8	<ul style="list-style-type: none">• The verification problem for a simple programming language• Symbolic execution
Week 9	<ul style="list-style-type: none">• Inductive invariants, verification conditions, and program correctness• Automatic invariant generation
Week 10	<ul style="list-style-type: none">• Proving program termination

Unit 4: Static Analysis and Abstract Interpretation

Reading: Chapters 2, 5 and 9 of (Møller and Schwartzbach, 2018)

Week 11	<ul style="list-style-type: none">• Predicate abstraction
Week 12	<ul style="list-style-type: none">• Counter-example guided abstraction refinement
Week 13	<ul style="list-style-type: none">• Fundamentals of dataflow analysis

Conclusion

Week 14	• Student project presentations
Week 15	• Course recap and research outlook

Potential Project Ideas

A small list of potential project ideas is attached below. Students are welcome to explore topics and papers not from the list, as long as they are related to the topic of the course and contain a strong research component. In any case, they are strongly encouraged to consult the instructor early and often, and keep him updated on their progress.

1. **Modeling the heap.** The toy programming languages used in the course will exclude pointers and dynamically allocated data (provided by the library functions `malloc` and `free`, and keywords `new` and `delete`). This limitation is not only pedagogical, as accurately describing the effects of these functions is an important research challenge in the field. Separation logic (O’Hearn et al., CSL 2001) is a particularly influential approach. One research project involves building solvers for various fragments of separation logic, such as that proposed by (Piskac et al., CAV 2014).
2. **Relational verification.** The view of verification taken in the course will mostly be whether each execution of a program individually satisfies some property. Unfortunately, this fails to capture many interesting program properties, including privacy (the output should not depend on some sensitive feature of the input) and robustness (small changes in the input should only trigger small changes in the output), where the property involves comparing the behavior of the program on two close-but-distinct inputs. Students can build program verifiers for such hyper-properties, basing their work on papers such as (Barthe et al., FM 2011).
3. **Symbolic execution and concurrency.** An important feature in the modern programming landscape is concurrency, where the program is composed of multiple threads which coordinate by mutating shared variables. Unfortunately, concurrent programs typically have a large number of possible thread interleavings, and this non-determinism makes symbolic execution hard. There is a wealth of research on analyzing such programs, for example (Wang et al., FSE 2009), which could form the basis of the course project.
4. **Min-UNSAT cores and maximum satisfiability.** The central problem we address in module 2 of the course is that of finding a satisfying assignment to a set of constraints. While a satisfying assignment is evidently immediately useful, reports of unsatisfiability clearly raise further questions. Users may wish to know: “Why was this problem instance unsatisfiable?”, or in several applications, may wish to follow up with, “Can we maximize the number of satisfied constraints?” These questions naturally point to the problems of finding UNSAT-cores and of Max-SAT respectively. These problems are the topic of intense research, and students may wish to use an existing SAT solver as a black box, and reproduce recent algorithms such as (Neves et al., SAT 2015).

5. **Randomly sampling solutions and model counting.** One prominent assumption we make in our discussion of SAT solvers is that we are content with arbitrary satisfying assignments. However, in many cases, such as in the verification of probabilistic programs and several applications in machine learning, this is insufficient, and users would like an algorithm which uniformly samples from the set of satisfying assignments. The problem of random solution sampling is closely related to the problem of finding the number of satisfying assignments to a given formula; this latter problem is the famous prototype of the #P complexity class. As with the previous project idea, students may use an existing SAT solver as a black box, and attempt to reproduce the algorithms described in (Chakraborty et al., AAI 2014) and related papers.

6. **Algorithms for synthesis.** Since the work on SyGuS, several new algorithms and frameworks have been developed for program synthesis. One important example has been the approach to combining top-down and bottom-up enumeration using a technique called unification (Alur et al., TACAS 2017). Another important question has been the notion of quantitative cost measures, such as the problem of finding the smallest or most high-performance solution. One algorithm is presented in (Hu and D'Antoni, CAV 2018). A third direction of research is in using learned syntactic features to accelerate the search for solution programs (Lee et al., PLDI 2018). Any of these papers would form a good basis for a course project.

Statement on Academic Conduct and Support Systems

Academic Conduct:

Plagiarism – presenting someone else’s ideas as your own, either verbatim or recast in your own words – is a serious academic offense with serious consequences. Please familiarize yourself with the discussion of plagiarism in SCampus in Part B, Section 11, “Behavior Violating University Standards” policy.usc.edu/scampus-part-b. Other forms of academic dishonesty are equally unacceptable. See additional information in SCampus and university policies on scientific misconduct, policy.usc.edu/scientific-misconduct.

Support Systems:

Counseling and Mental Health - (213) 740-9355 – 24/7 on call

studenthealth.usc.edu/counseling

Free and confidential mental health treatment for students, including short-term psychotherapy, group counseling, stress fitness workshops, and crisis intervention.

National Suicide Prevention Lifeline - 1 (800) 273-8255 – 24/7 on call

suicidepreventionlifeline.org

Free and confidential emotional support to people in suicidal crisis or emotional distress 24 hours a day, 7 days a week.

Relationship and Sexual Violence Prevention and Services (RSVP) - (213) 740-9355(WELL), press “0” after hours – 24/7 on call

studenthealth.usc.edu/sexual-assault

Free and confidential therapy services, workshops, and training for situations related to gender-based harm.

Office of Equity and Diversity (OED)- (213) 740-5086 | Title IX – (213) 821-8298

equity.usc.edu, titleix.usc.edu

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usc-advocate.symplicity.com/care_report

Avenue to report incidents of bias, hate crimes, and microaggressions to the Office of Equity and Diversity |Title IX for appropriate investigation, supportive measures, and response.

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uscsa.usc.edu

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Diversity at USC - (213) 740-2101

diversity.usc.edu

Information on events, programs and training, the Provost's Diversity and Inclusion Council, Diversity Liaisons for each academic school, chronology, participation, and various resources for students.

USC Emergency - UPC: (213) 740-4321, HSC: (323) 442-1000 – 24/7 on call

dps.usc.edu, emergency.usc.edu

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