



CSCI 599: Complexity

Units: 4

Spring 2023 Friday 1:00-4:20pm

Instructor: Jiapeng Zhang

Office Hours: TBA

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Course Description

Computational complexity theory focuses on understanding the fundamental limitations and capabilities of *efficient computation*. For example, which computational problems inherently require a huge amount of computational resources to solve, no matter how clever the algorithm? Typical resources include running time, running space/memory, and randomness. The most basic question of computational complexity is how to classify computational problems according to their difficulty. For example, the famous P vs. NP question asks whether the 3-SAT problem can be solved in polynomial time.

In this course, we will introduce some complexity classes, including P, NP, BPP, P/poly, and IP. We will also learn connections between complexity classes, and how to classify problems into appropriate classes. This course might be interesting to graduate students or advanced undergraduates, and in particular those who plan to do research in theoretical computer science.

Learning Objectives

The course is designed to enable students to:

1. Understand complexity classes, including P, NP, PSPACE, BPP, and classify computational problems into appropriate classes.
2. Understand reductions between computational problems, and understand NP-completeness.
3. Learn hardness results of some computational problems.

Recommended Preparation:

Knowledge of the material covered in CSCI 270 (or the equivalent). If you do not formally have this knowledge and still wish to take this course, please send me an email to discuss whether you should enroll in this course. The most important topics that we will assume from CSCI 270 are reductions, asymptotic running time, and NP-completeness. General mathematical skills including basic probability and combinatorics will also be assumed.

Textbook

We will use the book *Computational Complexity: A Modern Approach* by Sanjeev Arora and Boaz Barak.

Course Notes

Grading includes two parts:

- Three homework sets. (60%)
- A take-home final exam. (40%)

The problem sets will be challenging, so be sure to start them early. You are encouraged to collaborate the homework problems with each other in small groups (3 people), as long as you list all discussion partners on your problem set. Each group only needs to submit one copy of the solution. The take-home final exam should be solved independently.

Grading Breakdown

| Assessment Tool (assignments) | Points | % of Grade |
|-------------------------------|--------|------------|
| Homework | 60 | 60% |
| Final exam | 40 | 40% |
| | | |
| | | |
| | | |
| TOTAL | 100 | 100% |

Assignment Submission Policy

Homework and final exam should be submitted electronically.

Grading Timeline

Grading of each homework will be ready one week after submission.

Course Schedule: A Weekly Breakdown

| | Topics/Daily Activities | Readings/Preparation | Deliverables |
|---------------|---------------------------------------|----------------------|--------------|
| Week 1 | Introduction Computational models | Textbook: Section 1 | |
| Week 2 | Time complexity Hierarchy theorems | Textbook: Section 3 | |

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|----------------|--|----------------------|---|
| Week 3 | Reduction NP-completeness | Textbook: Section 2 | |
| Week 4 | Space complexity $PSPACE = NPSPACE$ | Textbook: Section 4 | HW 1: Due on Friday |
| Week 5 | Log-space $NL = coNL$ | Textbook: Section 4 | |
| Week 6 | Boolean circuit | Textbook: Section 6 | |
| Week 7 | Circuit lower bounds | Textbook: Section 6 | |
| Week 8 | Circuit lower bounds | Textbook: Section 6 | HW 2: Due on Friday |
| Week 9 | Randomness in computation | Textbook: Section 7 | |
| Week 10 | Randomness in computation | Textbook: Section 7 | |
| Week 11 | Randomness in computation | Textbook: Section 7 | |
| Week 12 | Interactive proofs | Textbook: Section 8 | HW 3: Due on Friday |
| Week 13 | $IP = PSPACE$ | Textbook: Section 8 | |
| Week 14 | Average-hardness One-way functions | Textbook: Section 10 | |
| Week 15 | Pseudorandom generators | Textbook: Section 16 | |
| FINAL | Final Exam | Final: Due on Friday | Refer to the final exam schedule in the <i>USC Schedule of Classes</i> at classes.usc.edu . |

Statement on Academic Conduct and Support Systems

Academic Conduct:

Plagiarism – presenting someone else’s ideas as your own, either verbatim or recast in your own words – is a serious academic offense with serious consequences. Please familiarize yourself with the discussion of plagiarism in SCampus in Part B, Section 11, “Behavior Violating University Standards” policy.usc.edu/scampus-part-b. Other forms of academic dishonesty are equally unacceptable. See additional information in SCampus and university policies on scientific misconduct, policy.usc.edu/scientific-misconduct.

Support Systems:

Counseling and Mental Health - (213) 740-9355 – 24/7 on call
studenthealth.usc.edu/counseling

Free and confidential mental health treatment for students, including short-term psychotherapy, group counseling, stress fitness workshops, and crisis intervention.

National Suicide Prevention Lifeline - 1 (800) 273-8255 – 24/7 on call
suicidepreventionlifeline.org

Free and confidential emotional support to people in suicidal crisis or emotional distress 24 hours a day, 7 days a week.

Relationship and Sexual Violence Prevention and Services (RSVP) - (213) 740-9355(WELL), press “0” after hours – 24/7 on call
studenthealth.usc.edu/sexual-assault

Free and confidential therapy services, workshops, and training for situations related to gender-based harm.

Office of Equity and Diversity (OED)- (213) 740-5086 | Title IX – (213) 821-8298
equity.usc.edu, titleix.usc.edu

Information about how to get help or help someone affected by harassment or discrimination, rights of protected classes, reporting options, and additional resources for students, faculty, staff, visitors, and applicants. The university prohibits discrimination or harassment based on the following *protected characteristics*: race, color, national origin, ancestry, religion, sex, gender, gender identity, gender expression, sexual orientation, age, physical disability, medical condition, mental disability, marital status, pregnancy, veteran status, genetic information, and any other characteristic which may be specified in applicable laws and governmental regulations. The university also prohibits sexual assault, non-consensual sexual contact, sexual misconduct, intimate partner violence, stalking, malicious dissuasion, retaliation, and violation of interim measures.

Reporting Incidents of Bias or Harassment - (213) 740-5086 or (213) 821-8298
usc-advocate.symplicity.com/care_report

Avenue to report incidents of bias, hate crimes, and microaggressions to the Office of Equity and Diversity |Title IX for appropriate investigation, supportive measures, and response.

The Office of Disability Services and Programs - (213) 740-0776

dsp.usc.edu

Support and accommodations for students with disabilities. Services include assistance in providing readers/notetakers/interpreters, special accommodations for test taking needs, assistance with architectural barriers, assistive technology, and support for individual needs.

USC Support and Advocacy - (213) 821-4710

uscса.usc.edu

Assists students and families in resolving complex personal, financial, and academic issues adversely affecting their success as a student.

Diversity at USC - (213) 740-2101

diversity.usc.edu

Information on events, programs and training, the Provost's Diversity and Inclusion Council, Diversity Liaisons for each academic school, chronology, participation, and various resources for students.

USC Emergency - UPC: (213) 740-4321, HSC: (323) 442-1000 – 24/7 on call

dsp.usc.edu, emergency.usc.edu

Emergency assistance and avenue to report a crime. Latest updates regarding safety, including ways in which instruction will be continued if an officially declared emergency makes travel to campus infeasible.

USC Department of Public Safety - UPC: (213) 740-6000, HSC: (323) 442-120 – 24/7 on call

dps.usc.edu

Non-emergency assistance or information.