## MATH 432 COMBINATORICS SPRING 2022 SYLLABUS

GRETA PANOVA

Location and meeting times: MWF 12-12:50, CPA 256 (in person, offline).

Instructor Office Hours: M 3:30-5 (in KAP), F 2:30-3:30 (in KAP), by appointment (over zoom), or via slack.

Teaching Assistant: TBA

**Course description.** This course is a broad introduction to *Combinatorics*, surveying a variety of topics and methods. We introduce some basic counting techniques (e.g. Pigeonhole principle, independence) and elementary proof techniques (e.g. mathematical induction and counting in two different ways). We apply these to basic enumeration of subsets, arrangements, and other similar structures with restrictions. We will also study generating functions and use them to enumerate more complex structures and solve recurrence relations. We study the basics of graph theory (e.g. colorings, matchings) and algorithms on graphs. Last, but not least, we will discuss basic computational complexity theory.

Learning Objectives. Our goal would be to develop problem solving skills and mathematical maturity by studying advanced counting techniques. By the end of the course, students should be able to write proofs, analyze basic enumeration questions and combinatorial algorithms, and being able to solve some problems concerning simple finite structures, somewhat similar in spirit to the "logic/quantitative puzzles" typical for software/finance industry interviews.

**Mode of instruction.** Lectures will take place in person in class at the scheduled times. Detailed schedule, material covered, pictures of the blackboard, notes and other materials will be uploaded on blackboard regularly. Course announcements will be posted on blackboard and emailed. Slack will be used for discussions.

Prerequisites: MATH 225 or MATH 226 or MATH 227.

**Course text and sources:** Homework, exam solutions, and supplementary notes will be available in Blackboard.

**Textbook:** Miklos Bona, *A Walk Through Combinatorics*, 4th edition.

Additional resources (freely available online): Richard Stanley "Enumerative Combinatorics Volume 1". Loren Larson "Problem-solving through problems".

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## GRETA PANOVA

**Grading.** Students are expected to complete weekly **problem sets**, whose goal is to reinforce and expand the topics covered in class in order to deepen the understanding, practice, learn. There will be 12 problem sets, each worth the same amount of points. The two lowest homework grades (including zeros for missing homeworks) will be dropped at the end. Homeworks will be generally **due on Wednesdays** uploaded on blackboard. Late assignments will be penalized by 20% per day.

There will be two in-class midterm exams, on February 16 and March 30, and a

final exam on Friday, May 6, 2-4pm.

## Score distribution

| Assignment                               | % Final Grade |
|--|---------------|
| Homeworks $(10 \text{ best out of } 12)$ | 25%           |
| Midterm I                                | 20%           |
| Midterm II                               | 20%           |
| Final Exam                               | 35%           |

Course Letter Grades: will be based on the total scores and determined "on a curve".

**Bonus problems** will be given regularly in homeworks. They will be more challenging, in the style of math olympiads/Putnam competition or brain teasers, and will not be counted towards the grade.

## **Preliminary Course Schedule of Topics:**

| Week/Date        | Topic  |
|------------------|--|
| Week 1, 01/10    | Methods of proof: contradiction, pigeonhole principle, in- |
|                  | duction  |
| Week 2, 01/17    | Elementary counting  |
| Week 3, 01/24    | Binomial theorem and identities                            |
| Week 4, 01/31    | Partitions and permutations                                |
| Week 5, 02/07    | Sieve methods, inclusion-exclusion                         |
| Week 6, 02/14    | Review and midterm I                                       |
| Week 7, 02/21    | Generating functions                                       |
| Week 8, 02/28    | Introduction to graph theory                               |
| Week 9, 03/07    | Trees, the matrix-tree theorem                             |
| Week 10, 03/14   | Spring break!!! :-)  |
| Week 11, 03/21   | Colorings and matchings                                    |
| Week 12, 03/28   | Review and midterm II                                      |
| Week 13, 04/04   | Planar graphs, Ramsey theory                               |
| Week 14, 04/11   | Probabilistic methods                                      |
| Week 15, 04/18   | Algorithms, computational complexity                       |
| Week 16, 04/25   | Problem solving as material review                         |
| Week 17, the end | Final exam on May 6  |