

EE575: Computational Differential Geometry for Engineers

Instructor: Anand A Joshi **Office:** EEB 426 **Email:** ajoshi@siipi.usc.edu

Schedule: Tu, Th; 12:30- 1:50 pm

Location: VKC203

Units: 3.0

Course Outline

Introduction, Partial differential equations, heat and Laplace equation, Numerical methods for their solutions. Theory of Curves tangents, arc-length, curvature, torsion, fundamental theorem of curves. Numerical representations of surfaces, Local theory of surfaces, parametric representation of surfaces, tangent plane. Mesh generation, marching cubes algorithm, surface parameterization, harmonic maps, conformal maps. Local theory of surfaces gauss map, Gaussian, mean and principle curvature. Some results on surfaces, curvature and geodesics. Conjugate gradient method, numerical methods for solving PDEs on surfaces. Laplacian on manifolds and its properties. Numerical spectral geometry, GPS surface representation. Smooth manifold, definition, properties, examples, theorems, differentiation on manifolds, integration. Riemannian metric, geodesics, tensors, covariant and contravariant tensors. Groups, Lie groups. Lie groups, $SO(3)$, Grassmannian, statistical manifold. Level Set Methods, geodesic active contours, geodesic curvature flow. Manifold learning methods, linear approaches, principle component analysis, multidimensional scaling, non-linear approaches, local linear embedding, ISOMAP. Shape analysis, Kendall's shape space and applications.

Recommended Preparation: The course is self-contained; however students should have a good background in calculus and familiarity with Matlab or C++.

Grading

1. *Homeworks* 30% 2. *Mid-Term Exam*: 30% (take home) 3. *Class Project*: 40%

There is no required test, the following texts are recommended references.

- A. M. Bronstein, M. M. Bronstein, R. Kimmel, Numerical geometry of non-rigid shapes, Springer, 2008.
- B. Lee, John M. Introduction to smooth manifolds. Vol. 218. Springer, 2012.
- C. Shifrin T, Differential Geometry: A First Course in Curves and Surfaces by. The book is free, and available online from <http://www.math.uga.edu/~shifrin/ShifrinDiffGeo.pdf>

Notice: Instructors reserve the right to make changes on this syllabus as needed