

# Partial Differential Equations

MATH 555a, Fall 2016

MWF 10-10:50am, KAP 134

**Instructor:** Juhi Jang

**Office:** KAP 416E

**e-mail:** juhijang@usc.edu

**Office hours:** 2-3pm on Wednesdays and 11-12pm on Fridays or by appointment

**Text:** *Partial Differential Equations by Evans* and class notes

**Course Description:** In this course, we will discuss classical methods used in the study of partial differential equations (PDEs). During the first two thirds of the course we focus on concrete examples of PDEs of different types: conservation laws, the transport equation, the heat equation, the porous media equation, the Laplace equation, and the wave equation. We will address various tools such as energy estimates, characteristics, similarity solutions, and fundamental solutions to study PDEs. During the last third of the course, we will learn the theory of Sobolev spaces, which is a fundamental tool in modern analysis of PDEs.

**Homework:** Homework will be assigned almost every other week. You are strongly encouraged to work on your homework on your own. If you use other sources, you are required to state them in the homework.

**Exam:** One in-class midterm (Wednesday, October 12) and one take-home final.

**Grade:** Homework (50%), Midterm (20%), Final (30%)

*Course information, assignments, and grades will be posted on Blackboard.*

## Tentative list of topics to be covered

### Introduction and Overview

Examples of PDEs

### Transport equation and Burger's equation

Linear transport equation; Burgers equation; Weak solution

### Laplace's equation and Poisson's equation

Fundamental solution; Poisson kernel; Green's function; Mean-Value property for Harmonic functions

## **Heat equation and Similarity solutions**

Fundamental solutions; Heat kernel; Maximum principle; Scaling; Fourier transform and its applications

## **Wave equations**

Spherical means; Finite speed of propagation

## **Sobolev spaces**

Approximation by smooth functions; Extensions and traces; Sobolev inequalities; Compactness; Difference quotients; Fourier transform methods

# **Statement on Academic Conduct and Support Systems**

## **Statement on academic integrity**

USC seeks to maintain an optimal learning environment. General principles of academic honesty include the concept of respect for the intellectual property of others, the expectation that individual work will be submitted unless otherwise allowed by an instructor, and the obligations both to protect one's own academic work from misuse by others as well as to avoid using another's work as one's own. All students are expected to understand and abide by these principles. SCampus, the Student Guidebook, contains the University Student Conduct Code (see University Governance, Section 11.00), while the recommended sanctions are located in Appendix A. Students will be referred to the Office of Student Judicial Affairs and Community Standards for further review, should there be any suspicion of academic dishonesty. The Review process can be found at: <http://www.usc.edu/student-affairs/SJACS/>.

## **Statement for students with disabilities**

Any student requesting academic accommodations based on a disability is required to register with Disability Services and Programs (DSP) each semester. A letter of verification for approved accommodations can be obtained from DSP. Please be sure the letter is delivered to me as early in the semester as possible. DSP is located in STU 301 and is open 8:30 a.m.-5:00 p.m., Monday through Friday. Website for DSP (<http://dsp.usc.edu>) and contact information: (213) 740-0776 (Phone).

## **Emergency preparation/course continuity in a crisis**

If an officially declared emergency makes travel to campus infeasible, USC Emergency Information <http://emergency.usc.edu> will provide safety and other updates, including ways in which instruction will be continued by means of blackboard, teleconferencing, and other technology.