A. F. J. Levi EE539: Engineering Quantum Mechanics. Fall 2010.

# Department of Electrical Engineering Engineering Quantum Mechanics. Fall 2010. TTh 11.00 a.m. – 12.20 a.m., KAP 166.

Web site: http://www.usc.edu/alevi Web site: http://web-app.usc.edu/soc/20103/ee.html Web site: http://www.usc.edu/students/enrollment/classes/term\_20103/

## **EE539:** Abstract and Prerequisites

Instructor: Office: Telephone: Email:	Tony Levi KAP 132 (213) 740-7318 alevi@usc.edu		<i>Office Hours:</i> TTh 8:00 a.m 9:30 a.m. or by appointment
<i>Grading:</i> Midterm Homework Final Exam		35% 10% 55%	<i>Final Exam:</i> 8:00 a.m 10:00 a.m., Tuesday, December 14, 2010, KAP 166

Required Text: Applied Quantum Mechanics A.F.J. Levi Cambridge University Press (2006) ISBN 9780521860963

Last day of class - Thursday, December 2, 2010

## Abstract

Quantum mechanics is the basis for understanding physical phenomena on the atomic and nanometer scale. There are numerous applications of quantum mechanics in biology, chemistry and engineering. Those with significant economic impact include semiconductor transistors, lasers, quantum optics and photonics. As technology advances, an increasing number of new electronic and opto-electronic devices will operate in ways that can only be understood using quantum mechanics. Over the next twenty years fundamentally quantum devices such as single-electron memory cells and photonic signal processing systems will become common-place. The purpose of this course is to cover a few selected applications and to provide a solid foundation in the tools and methods of quantum mechanics. The intent is that this understanding will enable insight and contributions to future, as yet unknown, applications.

## **Prerequisites**

Mathematics:

A basic working knowledge of differential calculus, linear algebra, statistics and geometry. *Computer skills:* 

An ability to program numerical algorithms in C, MATLAB, FORTRAN or similar language and display results in graphical form.

*Physics background:* 

Should include a basic understanding of Newtonian mechanics, waves and Maxwell's equations.

# **Introduction:** Lectures 1 - 3

## Lecture 1

*TOWARDS QUANTUM MECHANICS – PARTICLES AND WAVES* Diffraction, interference, and correlation functions for light Black-body radiation and evidence for quantization of light Photoelectric effect and the photon particle

## Lecture 2

Secure quantum communication The link between quantization of photons and quantization of other particles Diffraction and interference of electrons When is a particle a wave?

## Lecture 3

# THE SCHRÖDINGER WAVE EQUATION

The wave function description of an electron of mass  $m_0$  in free-space The electron wave packet and dispersion

The Bohr model of the hydrogen atom

Calculation of the average radius of an electron orbit in hydrogen Calculation of energy difference between electron orbits in hydrogen Periodic table of elements

Crystal structure

Three types of solid classified according to atomic arrangement Two-dimensional square lattice, cubic lattices in three-dimensions Electronic properties of semiconductor crystals The semiconductor heterostructure

## Using the Schrödinger wave equation: Lectures 4 - 6

## Lecture 4

## INTRODUCTION

The effect of discontinuities in the wave function and its derivative WAVE FUNCTION NORMALIZATION AND COMPLETENESS INVERSION SYMMETRY IN THE POTENTIAL

Particle in a one-dimensional square potential well with infinite barrier energy NUMERICAL SOLUTION OF THE SCHRÖDINGER EQUATION

Matrix solution to the descretized Schrödinger equation

Nontransmitting boundary conditions. Periodic boundary conditions

CURRENT FLOW

Current flow in a one-dimensional infinite square potential well Current flow due to a traveling wave

DEGENERACY IS A CONSEQUENCE OF SYMMETRY Bound states in three-dimensions and degeneracy of eigenvalues

## Lecture 5

BOUND STATES OF A SYMMETRIC SQUARE POTENTIAL WELL Symmetric square potential well with finite barrier energy

# TRANSMISSION AND REFLECTION OF UNBOUND STATES Scattering from a potential step when effective electron mass changes Probability current density for scattering at a step Impedance matching for unity transmission

#### Lecture 6

PARTICLE TUNNELING Electron tunneling limit to reduction in size of CMOS transistors THE NONEQUILIBRIUM ELECTRON TRANSISTOR

# **Scattering in one-dimension: The propagation method:** *Lectures* 7 - *10* Lecture 7

THE PROPAGATION MATRIX METHOD Writing a computer program for the propagation method TIME REVERSAL SYMMETRY CURRENT CONSERVATION AND THE PROPAGATION MATRIX

#### Lecture 8

THE RECTANGULAR POTENTIAL BARRIER Tunneling RESONANT TUNNELING Localization threshold Multiple potential barriers THE POTENIAL BARRIER IN THE δ-FUNCTION LIMIT

#### Lecture 9

ENERGY BANDS IN PERIODIC POTENTIALS: THE KRONIG-PENNY POTENTIAL Bloch's theorem Propagation matrix in a periodic potential

#### Lecture 10

THE TIGHT BINDING MODEL FOR ELECTRONIC BAND STRUCTURE Nearest neighbor and long-range interactions Crystal momentum and effective electron mass USE OF THE PROPAGATION MATRIX TO SOLVE OTHER PROBLEMS IN ENGINEERING THE WKB APPROXIMATION Tunneling

Related mathematics: Lecture 11 - 12 Lecture 11 ONE PARTICLE WAVE FUNCTION SPACE PROPERTIES OF LINEAR OPERATORS Hermitian operators Commutator algebra DIRAC NOTATION MEASUREMENT OF REAL NUMBERS Time dependence of expectation values. Uncertainty in expectation value The generalized uncertainty relation THE NO CLONING THEOREM

#### Lecture 12

DENSITY OF STATES Density of states of particle mass *m* in 3D, 2D, 1D and 0D Quantum conductance Numerically evaluating density of states from a dispersion relation Density of photon states

The harmonic oscillator: Lectures 13 - 14

#### Lecture 13

THE HARMONIC OSCILLATOR POTENTIAL CREATION AND ANNIHILATION OPERATORS The ground state. Excited states HARMONIC OSCILLATOR WAVE FUNCTIONS Classical turning point TIME DEPENDENCE The superposition operator. Measurement of a superposition state

#### Lecture 14

Time dependence in the Heisenberg representation Charged particle in harmonic potential subject to constant electric field *ELECTROMAGNETIC FIELDS* Laser light Quantization of an electrical resonator Quantization of lattice vibrations Quantization of mechanical vibrations

# Fermions and Bosons: Lecture 15 - 16

#### Lecture 15

INTRODUCTION

The symmetry of indistinguishable particles. Slater determinant Pauli exclusion principle. Fermion creation and annihilation operators – application to tight-binding Hamiltonian

#### Lecture 16

FERMI-DIRAC DISTRIBUTION FUNCTION Equilibrium statistics Writing a computer program to calculate the Fermi-Dirac distribution BOSE-EINSTIEN DISTRIBUTION FUNCTION **Time dependent perturbation theory and the laser diode:** *Lectures 17 - 21* Lecture 17

FIRST-ORDER TIME-DEPENDENT PERTURBATION THEORY Abrupt change in potential Time dependent change in potential CHARGED PARTICLE IN A HARMONIC POTENTIAL FIRST-ORDER TIME-DEPENDENT PERTURBATION

## Lecture 18

FERMI'S GOLDEN RULE IONIZED IMPURITY ELASTIC SCATTERING RATE IN GaAs The coulomb potential. Linear screening of the coulomb potential Correlation effects in position of dopant atoms Calculating the electron mean free path

#### Lecture 19

EMISSION OF PHOTONS DUE TO TRANSITIONS BETWEEN ELECTRONIC STATES

Density of optical modes in three dimensions

Light intensity

Background photon energy density at thermal equilibrium

Fermi's golden rule for stimulated optical transitions

The Einstein A and B coefficients

Occupation factor for photons in thermal equilibrium in a two-level system Derivation of the relationship between spontaneous emission rate and gain

## Lecture 20

THE SEMICONDUCTOR LASER DIODE

Spontaneous and stimulated emission

Optical gain in a semiconductor. Optical gain in the presence of electron scattering

# DESIGNING A LASER CAVITY

Resonant optical cavity. Mirror loss and photon lifetime The Fabry-Perot laser diode. Rate equation models

#### Lecture 21

NUMERICAL METHOD OF SOLVING RATE EQUATIONS

The Runge-Kutta method. Large-signal transient response. Cavity formation NOISE IN LASER DIODE LIGHT EMISSION

Effect of photon and electron number quantization

# **Time independent perturbation theory:** Lectures 22 - 23

Lecture 22

NON-DEGENERATE CASE Hamiltonian subject to perturbation W First-order correction. Second order correction Harmonic oscillator subject to perturbing potential in *x*, *x*<sup>2</sup> and *x*<sup>3</sup>

#### Lecture 23

DEGENERATE CASE Secular equation Two states Perturbation of two-dimensional harmonic oscillator Perturbation of two-dimensional potential with infinite barrier

# Angular momentum and the hydrogenic atom: Lectures 24 - 26

# Lecture 24

ANGULAR MOMENTUM Classical angular momentum The angular momentum operator Eigenvalues of the angular momentum operators  $L_z$  and  $L^2$ Geometric representation

## Lecture 25

SPHERICAL COORDINATES, SPHERICAL HARMONICS AND THE HYDROGEN ATOM

> Spherical coordinates and spherical harmonics The rigid rotator Quantization of the hydrogenic atom Radial and angular probability density

## Lecture 26

ELECTROMAGNETIC RADIATION

No eigenstate radiation Superposition of eigenstates Hydrogenic selection rules for dipole radiation Fine structure Hybridization