# AME 541:Linear Control Systems II

Time:	Th 6:30-9:10
Instructor:	H. Flashner
Office:	Olin Hall 430E
Phone:	(213) 740-0489
Office hours:	Tu10-12, W12-2
email	hflashne@usc.edu

Teaching Assistant: Hancheol Cho Office: VHE202

> *e-mail*: hancheol.cho@gmail.com Office hours: MW3-5

**Homework:** Will be assigned every Thursday and <u>must be submitted</u> the following Thursday

 ${\bf Grading:}\ {\bf The final grade will be assigned according to the following weightings:$ 

Homework:	20%
Midterm (October 20):	30%
Final (December 8, 7pm):	50%

### Textbook

J.P. Hespanha, Linear Systems Theory, Princeton Press, 2009.

## Reference books

- 1. C.T. Chen, *Linear Systems Theory and Design, 3rd Edition*, Oxford University Press, 1999.
- 2. F. Szidarowski and A. T. Bahill, Linear Systems Theory, CRC Press, 1992.
- 3. W. J. Rugh, Linear Systems Theory, Prentice-Hall, 1993.
- 4. T. Kailath, Linear Systems, Prentice-Hall, 1980.
- 5. K. Ogata, State Space Analysis of Control Systems, Prentice-Hall, 1967.

# <u>Outline</u>

1. Mathematical Representation of Systems (Notes)

(a) Modeling of dynamical systems

# 2. Linear Systems Modeling (Chapters 2-4)

- (a) State representation
- (b) Linearization
- (c) Realizations of transfer functions

## 3. Mathematical Background (Notes)

- (a) Linear spaces, norms, basis
- (b) Properties of matrices
- (c) Lyapunov equation
- (d) Singular value decomposition

# 4. Solution of State Equations (Chapter 5-7)

- (a) Properties of transition matrix
- (b) Computation of transition matrix for time-invariant systems
- (c) Equivalent Systems
  - i. Time-invariant systems
  - ii. Time-varying systems
- (d) Realizations
  - i. Time-invariant systems
  - ii. Time-varying systems
- (e) Discretization and solution od discrete-time equations

# 5. Stability Analysis (Chapters 8-9)

- (a) Input-output stability of LTI systems
- (b) Internal stability
- (c) Lyapunov theorem
- (d) Bounded-input, bounded output stability
- (e) Conditions for input-output stability

### 6. Controllability (Chapter 11-13)

- (a) Controllability and reachability: definitions and conditions
- (b) Controllable decomposition
- (c) Discrete systems

#### 7. Observability (Chapter 15-16)

- (a) Observability and constructability: definitions and conditions
- (b) Observable decomposition
- (c) Kalman decomposition

## 8. Minimal Realizations (Chapter 17)

- (a) Implications of of coprimness
- (b) Minimal realization of SISO systems
- (c) Balanced realization of SISO systems

## 9. Poles and Zeros of MIMO Systems (chapters 18-19)

- (a) Polynomial matrices: Smith form
- (b) Rational matrices: Smith-McMillan form
- (c) McMillan degree, poles and zeros
- (d) Transmission zeros and invariant zeros
- (e) Minimal realization of MIMO systems

# 10. State Feedback and State Observers (Chapter 14,16)

- (a) Stabilizability
- (b) Pole placement
- (c) Observers
- (d) Reduced-order observers.
- (e) Separation principle and output feedback

# 11. Linear Optimal Control (Chapter 20)

- (a) Quadratic performance indices
- (b) Riccatti equation
- (c) Robustness characteristics

# 12. Frequency Domain Analysis (Notes)